

9-2 Arithmetic Sequences

Objective:

- To define, identify, and apply arithmetic sequences

Common Core Content Standard:

F.1F.3 Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers.

A _____ is an ordered list of numbers.

An _____ sequence is a sequence where the difference between consecutive terms is constant. The difference is the _____ difference.

Take note

Key Concept Arithmetic Sequence

An arithmetic sequence with a starting value a and common difference d is a sequence of the form

$$a, a + d, a + 2d, a + 3d, \dots$$

A recursive definition for this sequence has two parts:

$$a_1 = a \quad \text{initial condition}$$

$$a_n = a_{n-1} + d, \text{ for } n > 1 \quad \text{recursive formula}$$

An explicit definition for this sequence is a single formula:

$$a_n = a + (n - 1)d, \text{ for } n \geq 1$$

Example 1: Identifying Arithmetic Sequences

Is the sequence an arithmetic sequence?

a. 12, 22, 32, 42, 52,

b. 1, 1, 2, 3, 5, ...

Example 2: Analyzing Arithmetic Sequences

What are the indicated terms of the arithmetic sequence?

a. the 110th term of the sequence that begins 5, 9, ...

b. the second and third terms of the sequence 90, ?, ?, 12, ...

The _____, or average, of the two numbers x and y is $\frac{x+y}{2}$. In an arithmetic sequence, the middle term of any three consecutive terms is the arithmetic mean of the other two terms.

Example 3: Using the Arithmetic Mean

What is the missing term of the arithmetic sequence ...35, ?, 53, ...?

Example 4: Using an Explicit Formula for an Arithmetic Sequence

Over the last ten years the amount of snow a town received formed an arithmetic sequence. If 21 in. of snow fell 10 years ago and 19 in. fell 9 years ago, how many inches fell 2 years ago?